For the requested seventh term the eight-term Cauchy product is already small. For a remote n, directly forming the weighted sum uses $n+1$ terms, while the proved formula reduces it to one Fibonacci value and scalar arithmetic. Fast doubling computes that Fibonacci value in $O(\log n)$ coefficient multiplications. The gain is for the generalized remote-index workload, not a claimed large runtime saving for $n = 7$.