The algorithm performs n length-n divisions and accumulations, hence $\Theta(n^2)$ in the stated implementation. Rebuilding every P_k independently by multiplying $n-1$ linear factors would cost $\Theta(n^3)$. For repeated value queries, barycentric evaluation avoids materializing coefficients, but that is a different output contract.