Four nonzero transitions suffice; a graph-based update takes four weighted contributions. A dense 3×3 update is also trivial. This question's optimal solution is direct transcription plus row-sum checks; no complex-analytic acceleration is warranted.