With rank vectors in RAM, each pass reads $O(N+E)$ graph records, performs $O(N+E)$ arithmetic, and uses $O(N)$ RAM plus the current adjacency list. With external vectors, each pass additionally incurs external-sort cost for E destination records. This is a genuine input/output complexity accounting; a dense transition matrix would require N^2 storage and violates the intended setting.