Reachability plus a teleport self-loop proves the recurrent-class claim in $O(N+E)$ graph work. The fixed-point iteration has the quantitative geometric bound already derived. A generic eigenvalue test is unnecessary to establish these structural facts.

Source qualification

The source statement is completed with an explicit reachable-support qualification and a counterexample to the unrestricted reading.