Comparative cost and preferred method

One analytic integration and a one-variable constrained minimum yield the best possible bound from the supplied envelope. Numerical quadrature would add approximation error and would not by itself certify optimality. This is an exact extremal result, not a measured speedup.