The thin SVD gives the full solution family and the minimum-norm representative in $O(pN^2)$ dense work. Enumerating nullspace coefficients is unnecessary when only the minimum-norm solution is required. The exact lower-dimensional solve is also the appropriate conventional method.