For a length-N spectrum, all four transformed outputs can be obtained with reversal, conjugation, additions and scales in $O(N)$ work, avoiding four new FFTs. The source's false part is replaced only after it has been explicitly disproved.

Source qualification

The missing conjugation is present in the visually inspected printed statement, not introduced by this transcription.